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## Introduction \& Problem Formulation

Goal: To reduce the word embedding size in pre-trained language models by representing each word with composition of $f$ low-dimensional embeddings shared between vocabulary.

## Spotlight:

- Substantially alleviates the number of embedding parameters in the embedding part through Cartesian product.
- Solves the out-of-vocabulary problem in the (masked) language models.
- Subspace embeddings achieve compression rates beyond $99.8 \%$ in comparison with the original embeddings for the language models on XNLI and GLUE benchmark suites.


## Problem Settings:

- Subspace Embedding (SE) describes the latent space of contextual elements within a token, where each element composes to form the original embedding.
- SE create an arbitrary-sized vector of each word that incorporates semantic relationships.
- We arbitrarily assign the subspace embedding to each token based on its index and perform a Cartesian product with subspace embedding to construct embedding vectors



## - Calibration of Subspace Embedding:

- Original embedding vectors: $E_{i}, E_{j}$, their SE vectors: $\left\{v_{i}^{f}\right\},\left\{v_{j}^{f}\right\}, \forall i, j \in\{1,2, \ldots, D\}$
- Conditions for uniqueness of partitioned embedding vectors: $f \in\{1,2, \ldots, F\}$ such that $\left\{v_{i}^{f}\right\} \neq\left\{v_{j}^{f}\right\}$ and $i \neq j$
- A mapping function to transform original embeddings to subspace embeddings, $\mathcal{F}: \mathcal{P} \rightarrow \mathcal{Q} \times \ldots \times \mathcal{Q}$, where a set of the embedding index as $\mathcal{P} \in\{1,2, \ldots, D\} \subset \mathrm{N}$ and $\mathcal{Q}=\{1,2, \ldots, Q\} \subset \mathrm{N}$ depicts a set of each SE vector index
- Generalise via Cartesian product, $\mathcal{F}(n)=\left(c_{1} \times c_{2} \times\right.$

$$
\left.\times c_{f}\right) \overbrace{(n, \ldots, n)}^{f}
$$

- We have $f$ distinct $Q \times(d / f)$ embedding table, where each subspace
- Subspace embedding representation, $v_{n}=$ $\oplus_{f=1, \ldots, F} v_{c_{f}(n)}$, where $v_{n}, v_{c_{f}}$ are the corresponding embedding vectors and $\oplus$ denotes the concatenation operation.


## Contributions

A word embedding compression method for pre-trained language models (PLMs) that

- allocates shared subspace embedding to the embedding vector in two ways:
- It allocates sequentially using modulo operation
- It assigns dispersed subspace embedding using a pretrained language model with contextual information


## Our Approach \& Experiments

Techniques for Embedding Compression:

| Algorithm 1 Assign Subspace Embedding Arbitra |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Input: $D$ number of embeddings with dimension $d$, and set of subspace embeddings $F$ <br> 1: $Q \leftarrow\left\lceil D^{1 / f}\right\rceil \quad \Delta$ number of each subspace embedding <br> 2: Initialise $f$-th $Q$ subspace embedding vectors $\left\{v_{q}^{f} \in \mathrm{R}^{\frac{d}{f}}\right\}_{q=1}^{Q}, \forall f$ $\{1, \ldots, F\}$ <br> for $n=1,2, \ldots, D$ do <br> for $\mathrm{f}=1,2, \ldots, F$ do <br> $c_{f}(n)=\left(n / Q^{f-1}\right) \bmod Q^{f}$ <br> end for <br> $v_{n}=\oplus_{f=1}^{F} v_{c_{f}(n)}$ <br> end for <br> Output: The incorporated embedding vectors are $\left\{v_{n}\right\}_{n=1}^{D}$. |  |  |  |  |
| Language Model Settings: <br> Table 1: Description of the altered neural language models. |  |  |  |  |
| NLMs | Vocabulary Size | \# Embeddings | $\|\theta\|$ | $\left\|\theta_{v}\right\|$ |
| RoBERTas | 50k | 50k | 51M | 25. |
| +2-S | 50k | 225 | 26M | 115k |
| +3-SE | 50k | 37 | 26M | 18 |
| +8-SE | 50k |  | 26M | 2k |
| XLM-R ${ }_{\text {S }}$ | 250k | 250k | 154 | 128 |
| -SE | 250k | 63 | 26M | 32k |

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Algorithm 2 Cluster-based Subspace Embedding
Input: \(D\) number of embeddings, \(Q\) number of subspace embeddings, \(d\) dimension of embedding, and number of subspace embeddings set \(F\) the pre-trained embedding model \(\mathcal{L}_{P}=\left\{p_{n}\right\}_{n=1}^{D}\)
1: Initialise \(f\)-th \(Q\) subspace embedding vectors \(\left\{v_{q}^{f} \in \mathbb{R}^{\frac{d}{f}}\right\}_{q=1}^{Q}, \forall f \in\) \(\{1, \ldots, F\}\)
2: \(c_{f}(n) \leftarrow 0, \forall f=1, \ldots, F, n=1, \ldots, D\)
3: for \(f=1,2, \ldots, F\) do
4: \(\quad\) extract distinct tuples from \(\{\mathcal{F}(n)\}_{n=1}^{D}\)
for distinct \(\mathcal{F}\left(n^{*}\right)\) in \(\{\mathcal{F}(n)\}_{n=1}^{D}\) do if \(f \neq F\) then
\(\left\{\mathcal{L}_{P}\right\}_{\mathcal{F}\left(n^{*}\right)} \leftarrow\left\{p_{n}: \mathcal{F}(n)=\mathcal{F}\left(n^{*}\right)\right\}_{n=1}^{D}\)
alter k-means algorithm to \(\left\{\mathcal{L}_{P}\right\}_{\mathcal{F}\left(n^{*}\right)}\)
the outcomes labelling to \(c_{f}(n)\), where \(\mathcal{F}(n)=\mathcal{F}\left(n^{*}\right)\) else
\(c_{f}(n) \leftarrow\) arbitrary number among \(Q\) candidates end if
end for
14: end for
15: Collect \(v_{n}=\oplus_{f=1}^{F} v_{c_{f}(n)}, \forall n \in P\)
Output: The incorporated embedding vectors are \(\left\{v_{n}\right\}_{n=1}^{D}\)
```

Results on the GLUE Benchmark:
Table 2: Results of Arbitrarily Dispersed Subspace Embed-
ding on GLUE. Columns in blue colour follow Algorithm 1.
Table 3: Results of the Algorithm 2 on GLUE. Shaded columns

| Dataset Model RoBERTas (Ours) |  | +2-SE | +3-SE | +4-SE | +6-SE | +8-SE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 6 | 8 |
|  | 50k | 225 | 37 | 15 | 7 | 4 |
| SST-2 [21] | 89.8 | 88.4 | 88.0 | 88.1 | 87.2 | 88.0 |
| Quora Questions ${ }^{3}$ | 86.5 | 84.0 | 83.0 | 83.3 | 82.6 | 83.0 |
| MNLI [28] | 79.5 | 74.3 | 73.1 | 72.8 | 73.5 | 73.0 |
| QNLI [19] | 88.1 | 84.0 | 83.4 | 84.1 | 84.1 | 83.0 |
| MRPC [9] | 88.3 | 88.0 | 85.5 | 87.4 | 85.2 | 86.3 |
| RTE [8] | 72.8 | 66.9 | 67.8 | 70.0 | 67.4 | 67.8 |
| STS-B [3] | 88.0 | 79.2 | 77.3 | 78.4 | 79.5 | 76.4 |
| CoLA [26] | 38.0 | 35.6 | 18.5 | 23.2 | 25.5 | 20.0 |

means, and uniform cluster size.

| Dataset Model | RoBERTas (Ours) | +2-SE | +3-SE | +3-SE | +3-SE | +3-SE | +3-SE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | , | 2 | 3 | 3 | 3 | 3 | 3 |
|  |  |  |  | $\mathrm{Q}=100$ | $\mathrm{Q}=200$ | Q=50 | Q=100 |
| $\left\|\theta_{0}\right\|$ | 25.7M | 115k | 18.9k | 104k | 154k | 25.6k | 51.2k |
| \% $\downarrow$ |  | 99.5 | 99.93 | 99.6 | 99.3 | 99.87 | 99.8 |
| SST-2 [21] | 89.8 | 88.4 | 88.0 | 88.2 | 90.0 | 89.3 | 89.3 |
| Quora Questions ${ }^{4}$ | 86.5 | 84.0 | 83.0 | 84.7 | 85.6 | 84.5 | 84.6 |
| MNLI [28] | 79.5 | 74.3 | 73.1 | 75.9 | 77.5 | 75.8 | 77.2 |
| QNLI [19] | 88.1 | 84.0 | 83.4 | 85.1 | 85.5 | 83.5 | 85.8 |
| MRPC [9] | 88.3 | 88.0 | 85.5 | 87.3 | 88.6 | 87.7 | 87.3 |
| RTE [8] | 72.8 | 66.9 | 67.8 | 67.1 | 69.7 | 67.9 | 70.7 |
| STS-B [3] | 88.0 | 79.2 | 77.3 | 81.6 | 84.5 | 80.1 | 84.8 |
| CoLA [26] | 38.0 | 35.6 | 18.5 | 37.5 | 34.9 | 33.6 | 36.7 |

Results on Multilingual dataset: We use the XLM-R model based on the Unicoder [3] to evaluate a cross-lingual transfer task. Our altered XLM-R ${ }_{S}$ network with 250 k and 63 number of embeddings for 3-SE, and 128 for clustered SE. The performances on English dataset are $74 \%, 72.6 \%$, and $72.9 \%$ for $\mathrm{XLM}_{S}, 3-\mathrm{SE}$, and clustered SE.
Conclusion and Future Work:

- Introduced a novel compact embedding structure, which significantly reducing the number of parameters in neural language models
- We intend to test and scale our embedding compression techniques on LLMs, catering over 200M parameters.
- We evaluated our compact embedding structure on English/Multilingual datasets. Our main structure of the pre-trained language model for downstream tasks follows RoBERTa [1]. Also, we employ XLM-R [2] for performance tests of subspace embedding on multilingual datasets.
References:
[1] Liu, Y., Ott, M., Goyal, N., Du, J., Joshi, M., Chen, D., ... \& Stoyanov, V. (2019). Roberta: A robustly optimized bert pretraining approach. arXiv preprint arXiv:1907.11692.
[2] Conneau, A., Khandelwal, K., Goyal, N., Chaudhary, V., Wenzek, G., Guzmán, F., ... \& Stoyanov, V. (2020, July). Unsupervised Cross-lingual Representation Learning at Scale. In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics (pp. 8440-8451).
[3] Huang, H., Liang, Y., Duan, N., Gong, M., Shou, L., Jiang, D., \& Zhou, M. (2019, November). Unicoder: A Universal Language Encoder by Pre-training with Multiple Cross-lingual Tasks. In Proceedings of the 2019 Conference on Empirical Methods in Natural Language Processing and the 9th International Joint Conference on Natural Language Processing (EMNLP-IJCNLP) (pp. 2485-2494).

